

Introduction to the mathematical description of water waves

References and Reading List

The books, research texts and papers are listed alphabetically under the various headings relevant to the material covered in the lectures. Because of the number, a few are starred that you might want to look at first.

Fluids dynamics

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- Lamb, H., *Hydrodynamics*, Cambridge Univ. Press, Cambridge, 1895 (many reprints).
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Water waves

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Constantin, A., *Nonlinear water waves with applications to wave-current interactions and tsunamis*, SIAM CBMS-NSF Regional Conference Series in Applied Mathematics, **81**, SIAM, Philadelphia, 2011.

Craik, A.D.D., The origins of water wave theory, *Ann. Rev. Fluid Mech.*, **36**, 1-28, 2004.

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Okamoto, H. & Shoji, M., *The mathematical theory of permanent progressive water waves*, World Scientific, New Jersey, 2001.

*Stoker, J.J., *Water waves: the mathematical theory with applications*, Interscience, New York, 1957.

and this may be of interest (old, but contains many pictures and descriptions):

Cornish, V., *Waves of the Sea and other Water Waves*, T. Fisher Unwin, London, 1910.

Soliton theory

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Singular perturbation theory

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Solitary wave

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Gerstner's wave

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Korteweg-de Vries equation for a shear flow: critical layers & Cat's-eyes

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Edge waves

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